Lecture 4: Model checking



"perhaps the most important part of applied statistical" modelling"

Simon Wood

Model checking

- As with detection functions, checking is important
- Checking *doesn't* mean your model is **right**
- Want to know the model conforms to assumptions
- What assumptions should we check?

Convergence

Convergence

- Fitting the GAM involves an optimization
- By default this is REstricted Maximum Likelihood (REML) score
- Sometimes this can go wrong
- R will warn you!

A model that converges

gam.check(dsm_tw_xy_depth)

```
##
## Method: REML Optimizer: outer newton
## full convergence after 7 iterations.
## Gradient range [-3.456333e-05,1.051004e-05]
## (score 374.7249 & scale 4.172176).
## Hessian positive definite, eigenvalue range [1.179219,301.267].
## Model rank = 39 / 39
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
              k' edf k-index p-value
##
## s(x,y) 29.00 11.11 0.65 <2e-16 ***
## s(Depth) 9.00 3.84 0.81 0.37
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

A bad model

Error in while (mean(ldxx/(ldxx + ldss)) > 0.4) { :
 missing value where TRUE/FALSE needed
In addition: Warning message:
In sqrt(w) : NaNs produced
Error in while (mean(ldxx/(ldxx + ldss)) > 0.4) { :
 missing value where TRUE/FALSE needed

This is **rare**

The Folk Theorem of Statistical Computing

"most statistical computational problems are due not to the algorithm being used but rather the model itself"

Andrew Gelman

Folk Theorem anecdata

- Often if there are fitting problems, you're asking too much from your data
- Model is too complicated
- Too little data (check n in summary, is it right?)
- Try something simpler, see what happens

Basis size

Basis size (k)

- Set k per term
- e.g. s(x, k=10) or s(x, y, k=100)
- Penalty removes "extra" wigglyness
 up to a point!
- (But computation is slower with bigger k)

Checking basis size

gam.check(dsm_x_tw)

##

```
## Method: REML Optimizer: outer newton
## full convergence after 7 iterations.
## Gradient range [-3.196351e-06,4.485625e-07]
## (score 409.936 & scale 6.041307).
## Hessian positive definite, eigenvalue range [0.7645492,302.127].
## Model rank = 10 / 10
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
## k' edf k-index p-value
## s(x) 9.00 4.96 0.76 0.38
```

Increasing basis size

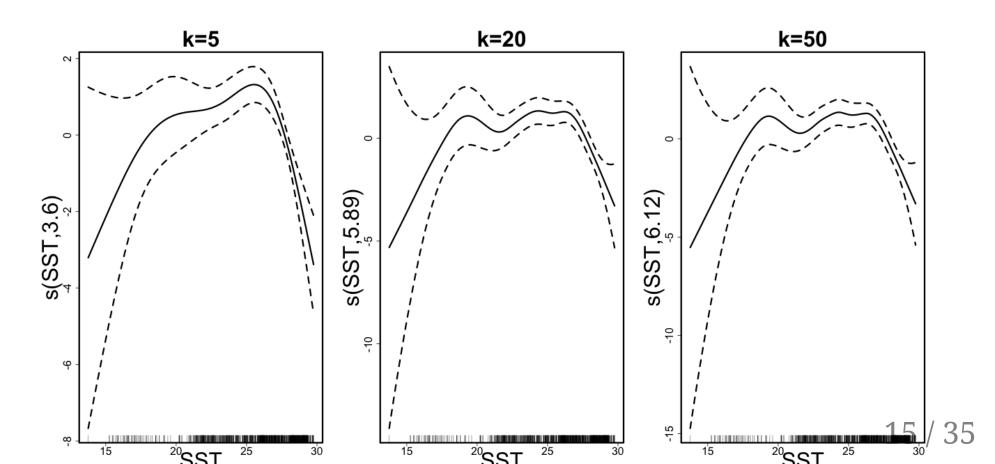
```
##
## Method: REML Optimizer: outer newton
## full convergence after 7 iterations.
## Gradient range [-2.30124e-08,3.930703e-09]
## (score 409.9245 & scale 6.033913).
## Hessian positive definite, eigenvalue range [0.7678456,302.0336].
## Model rank = 20 / 20
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
## k' edf k-index p-value
## s(x) 19.00 5.25 0.76 0.35</pre>
```

Sometimes basis size isn't the issue...

- Easy rule:
 - double k and see what happens
- Didn't increase the EDF much here
- Other things can cause low "p-value" and "k-index"
- Increasing k increases computing time

k is a maximum

- Don't worry about things being too wiggly
- k gives the maximum complexity
- Penalty deals with the rest



Residuals

What are residuals?

- Residuals = (observed value) (fitted value)
- BUT hard to see patterns in these "raw" residuals
- Need to standardise ⇒ deviance residuals
- Expect these residuals ~ N(0, 1)

Why are residuals important?

- Structure in the residuals means your model didn't capture something
- Maybe a missing covariate
- Model doesn't describe the data well

Fitting to residuals

- Refit our model but with the residuals as response
- Response is normal (for deviance residuals)
- What pattern is left in the residuals?

Example

• Example model with NPP and Depth

summary(resid_fit)

```
##
## Family: gaussian
## Link function: identity
##
## Formula:
## resid ~ s(Depth, bs = "ts", k = 20) + s(NPP, bs = "ts", k = 20)
##
## Parametric coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49454 0.03274 -15.1 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
##
               edf Ref.df F p-value
## s(Depth) 2.56621 19 1.230 4.9e-06 ***
## s(NPP) 0.03322 19 0.002 0.316
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
\#\# R-sq.(adj) = 0.0241 Deviance explained = 2.67%
## -REML = 1362 Scale est. = 1.0174 n = 949
```

What's going on there?

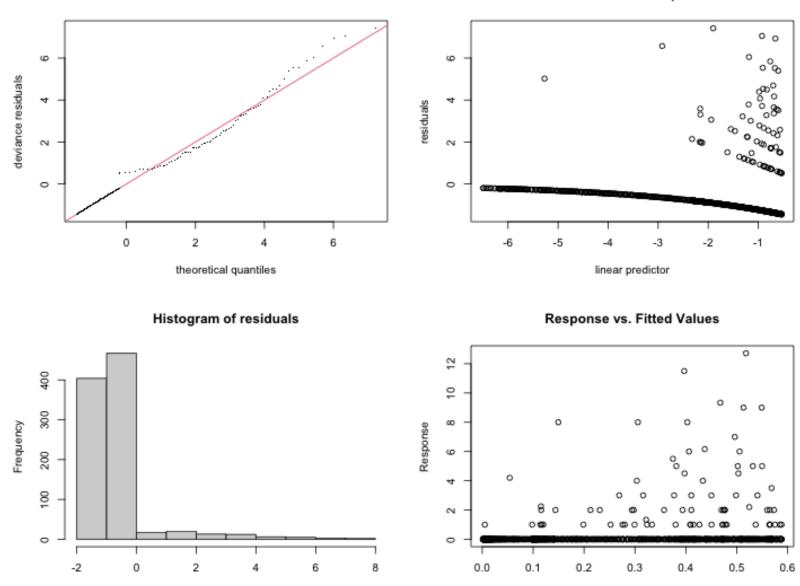
- Something unexplained going on?
- Maybe Depth + NPP is not enough?

• Add other smooths (s(x, y)?)

• Increase k?

Other residual checking

gam.check



Resids vs. linear pred.

Eliteral Markers

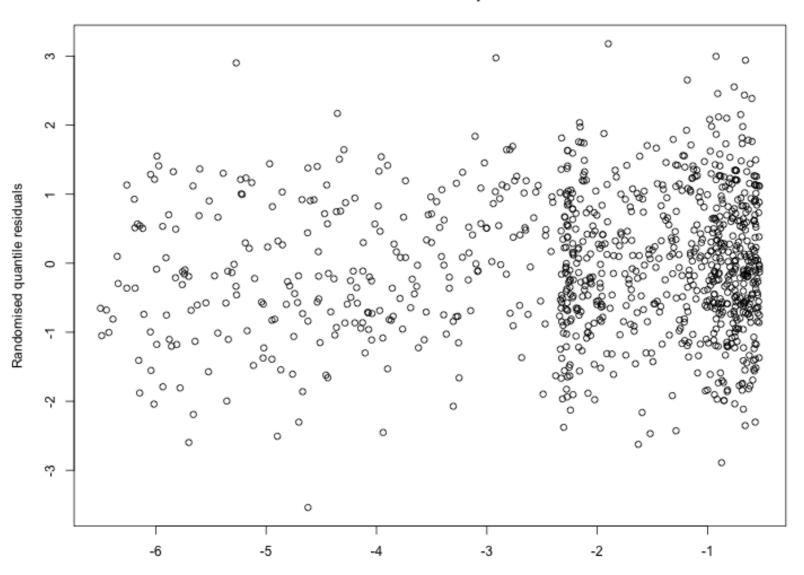
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Desidente

Shortcomings

- gam.check can be helpful
- "Resids vs. linear pred" is victim of artifacts
- Need an alternative
- "Randomised quanitle residuals"
 - o rqgam.check
 - Exactly normal residuals

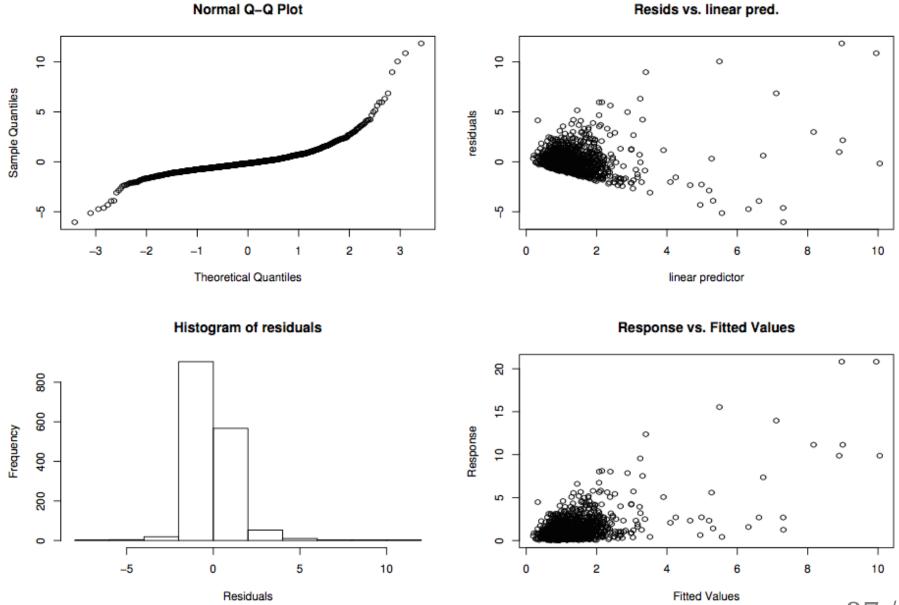
Randomised quantile residuals



Resids vs. linear pred.

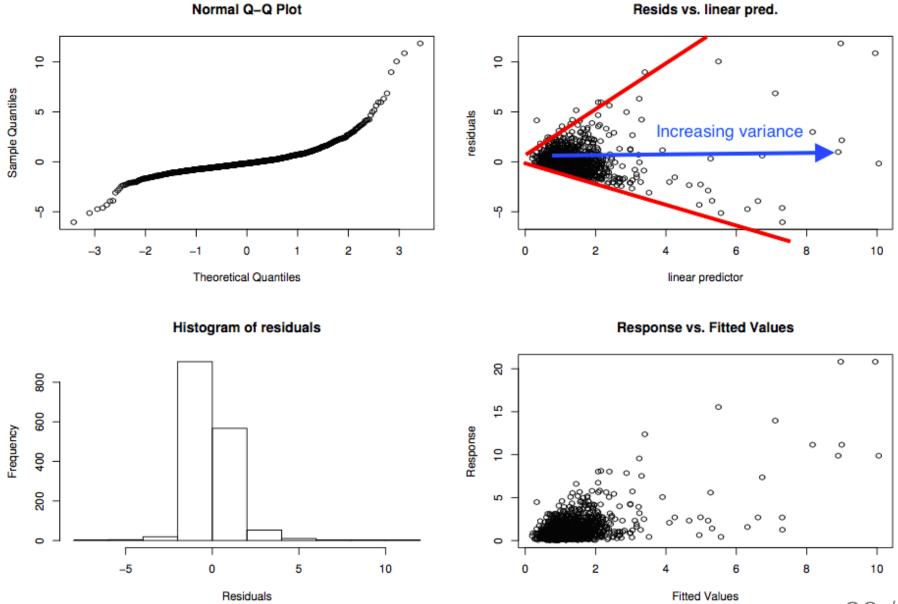
linear predictor

Example of "bad" plots



```
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```

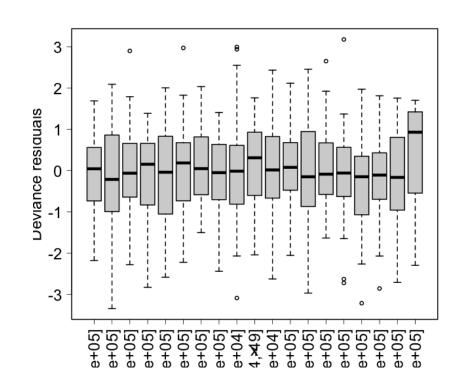
Example of "bad" plots



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Looking for artefacts

- Want to avoid "pattern" in residuals
- How to visualise?
- Plot residuals vs. covariates
- Should look like this



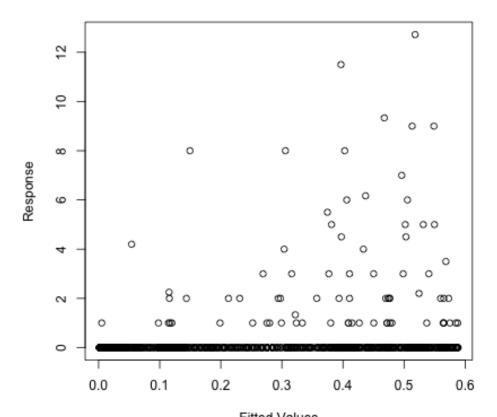
Residual checks

- Looking for patterns (not artifacts)
- This can be tricky
- Need to use a mixture of techniques
- Cycle through checks, make changes recheck

Observed vs. expected

Response vs. fitted values

- gam.check "response vs. fitted values"
- BUT smooths are "wrong" everywhere in particular (but "right" on average!)



Response vs. Fitted Values

Summarize over covariate chunks

- On average the smooth is right
- Check aggregations of count
- Here detection function has Beaufort as factor

obs_exp(dsm_bad, "Beaufort_f")

[0,1] (1,2] (2,3] (3,4] (4,5]
Observed 1.00000 95.45000 103.5500 34.70000 4.000000
Expected 20.28781 54.57573 136.3581 53.98742 5.949304

obs_exp(dsm_good, "Beaufort_f")

[0,1] (1,2] (2,3] (3,4] (4,5]
Observed 1.0000 95.45000 103.5500 34.70000 4.000000
Expected 6.8887 45.18587 118.5747 53.81458 4.909644

Observed vs. expected for environmental covariates

• Just need to specify the cutpoints

obs_exp(dsm_bad, "Depth", c(0, 1000, 2000, 3000, 4000, 6000))
(0,1e+03] (1e+03,2e+03] (2e+03,3e+03] (3e+03,4e+03] (4e+03,6e+03]
Observed 4.00000 52.53333 139.16667 35.00000 8.00000
Expected 85.65231 37.98341 63.40892 53.78726 30.32642

obs_exp(dsm_good, "Depth", c(0, 1000, 2000, 3000, 4000, 6000))

##	(0,1e+03]	(1e+03,2e+03]	(2e+03,3e+03]	(3e+03,4e+03]	(4e+03,6e+03]
## Observed	4.000000	52.53333	139.1667	35.00000	8.00000
## Expected	5.308628	48.14915	128.7962	38.76013	8.359456

Summary

- Convergence
 - Rarely an issue
- Basis size
 - k is a maximum
 - Double and see what happens
- Residuals
 - Deviance and randomised quantile
 - check for artifacts
- Observed vs. expected
 - Compare aggregate information