

# Estimation with incomplete detection at distance zero

## “ $g(0) < 1$ ”

**Chapter 6 of Advanced book** (Methods for incomplete detection at distance zero by Laake and Borchers)

Borchers, D., Laake, J., Southwell, C. and Paxton, C. 2006. Accommodating unmodeled heterogeneity in double-observer distance sampling surveys. *Biometrics* **62**: 372-378

Buckland, S.T., Laake, J.L. and Borchers, D.L. 2009. Double-observer line transect methods: levels of independence. *Biometrics* **66**: 169-177

Laake, J.L., Collier, B.A., Morrison, M.L. and Wilkins, R.N. 2011. Point-based mark-recapture distance sampling. *JABES* **16**: 389-408

Burt, M.L., Borchers, D.L., Jenkins, K.J. and Marques, T.A.M. 2014. Using mark-recapture distance sampling methods on line transect surveys. *Methods in Ecology and Evolution* **5**: 1180-1191.

Conventional Distance sampling estimates are  
biased if  $g(0) < 1$ :

$$D^* = D \times g(0)$$

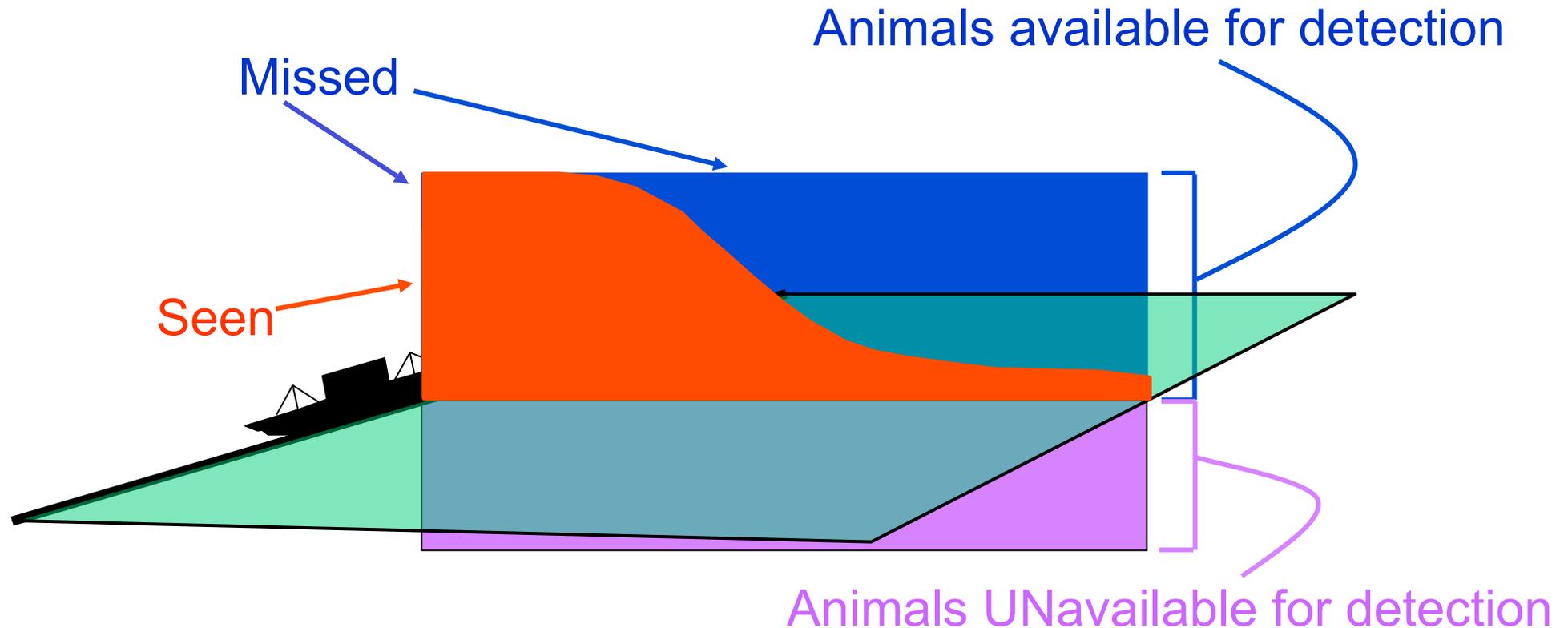
where  $D$  is the true density and  $D^*$  is the density obtained if you  
assume  $g(0) = 1$ .

$g(0) < 1$  when there is

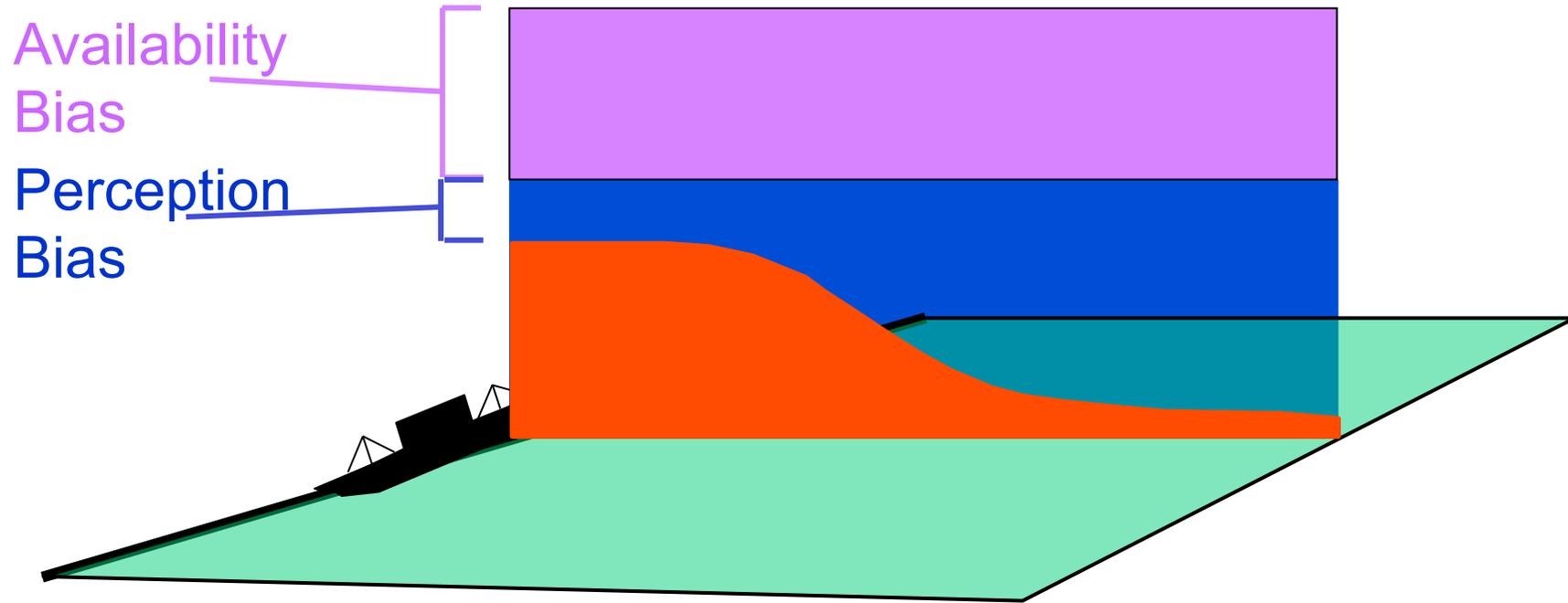
**Availability Bias**

**Perception Bias at distance 0**

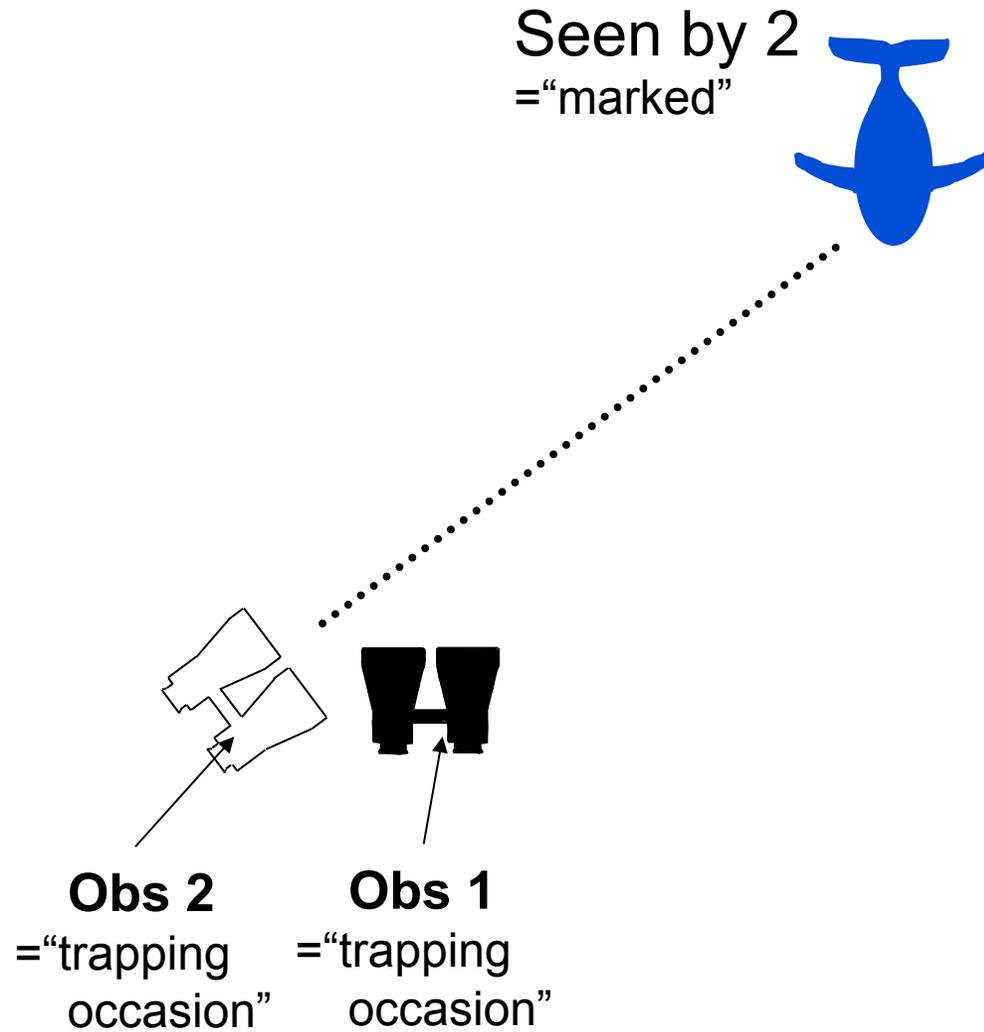
- “**Availability Bias**”: When animals are unavailable for detection.
- “**Perception Bias**”: When observers fail to detect animals **at distance 0** although they are available



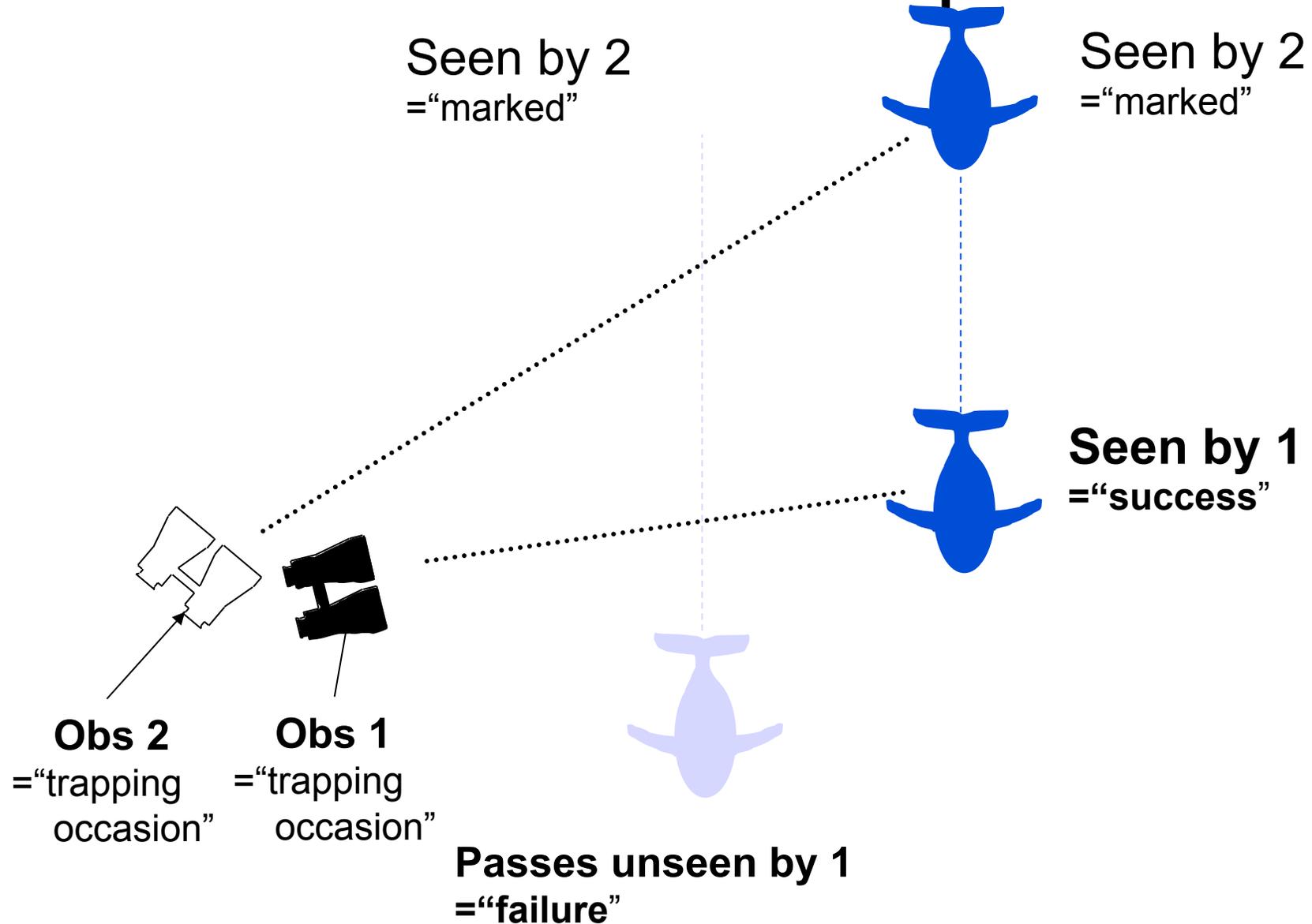
- “**Availability Bias**”: When animals are unavailable for detection.
- “**Perception Bias**”: When observers fail to detect animals **on the transect** although they are available



# Visual Mark-Recapture



# Visual Mark-Recapture



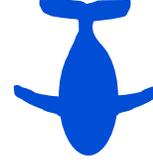
# Visual Mark-Recapture

Seen by 2  
="marked"



Passes unseen by 1  
="failure"

Seen by 2  
="marked"

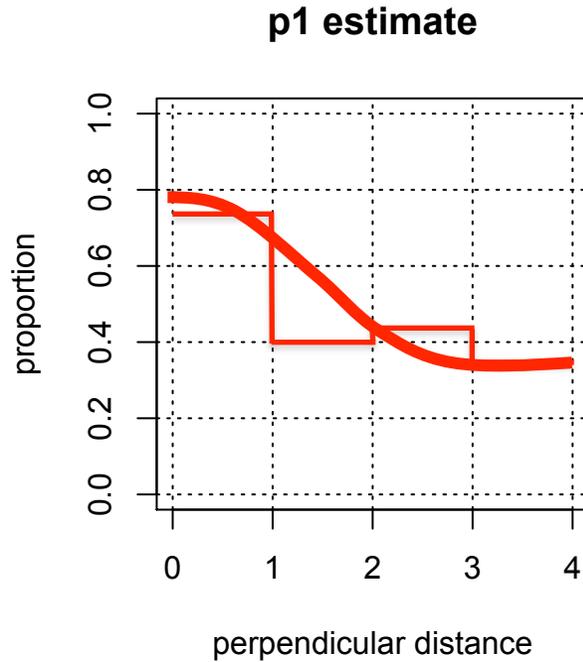
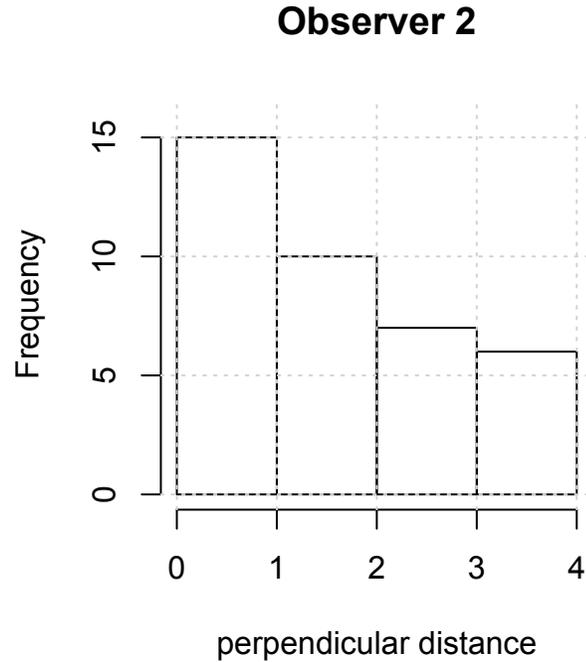


Seen by 1  
="success"

- We know 2 animals passed (because Obs 2 saw them)
- Of these, Obs 1 saw 1
- So **estimate:**  
$$\Pr(\text{Obs 1 sees}) = \hat{p}_1 = \frac{1}{2} = \frac{n_{12}}{n_2} = \frac{\text{number "duplicates"}}{\text{number seen by 2}}$$

Note: In this section, we use  $p$ , not  $g$  for the detection function

# Class Exercise



**Obs 2 detections:**

100s: 101,102,103,104,105,106 107 108,111 112,114,115,116 118,134  
200s: 201 202 204 205 206 207 211 214 215,218  
300s: 301,303 304,305,307 313,314  
400s: 402,404 407 416 417 418

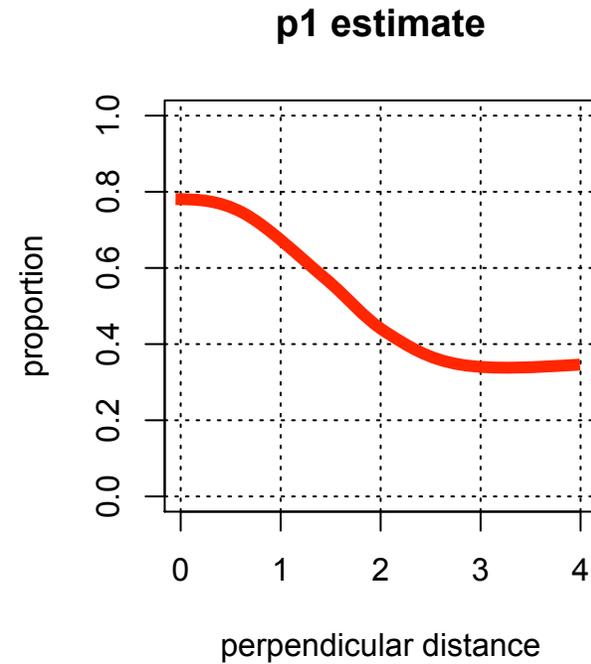
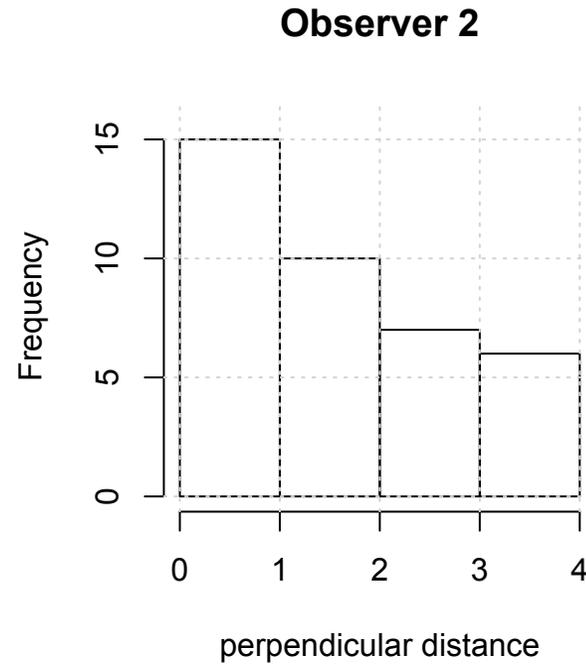
$n_2$	$\hat{p}$	$n_1$	$\hat{N}_x$
15			
10			
7			
6			

$n_{dups} = 20$

38                      25

$$\hat{N}_{Petersen} = \frac{n_1}{\hat{p}_1} = \frac{25}{20 / 38} = 47.5$$

$\hat{N}_{TOTAL} =$



Fit smooth curve using Logistic Regression  
(instead of grouping into distance intervals)

# Duplicate Identification

## Field methods

- Use a dedicated “duplicate identifier”
- Record measure of confidence in duplicate identification.
- Record positions and times as precisely as possible
- Record ancillary data
- Have at least one observer “track” animals

# Duplicate Identification

## Analysis methods

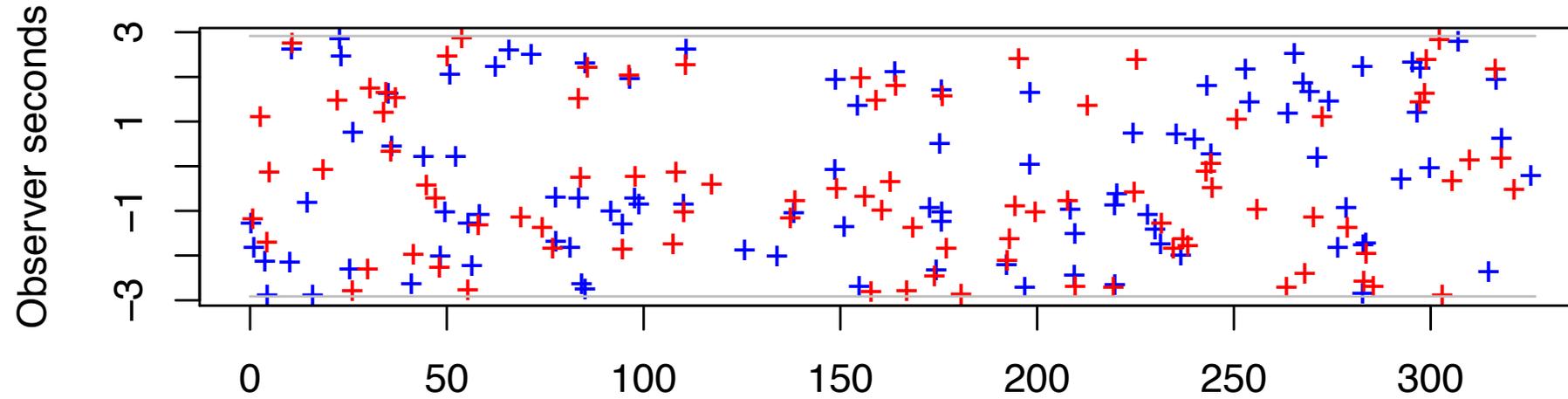
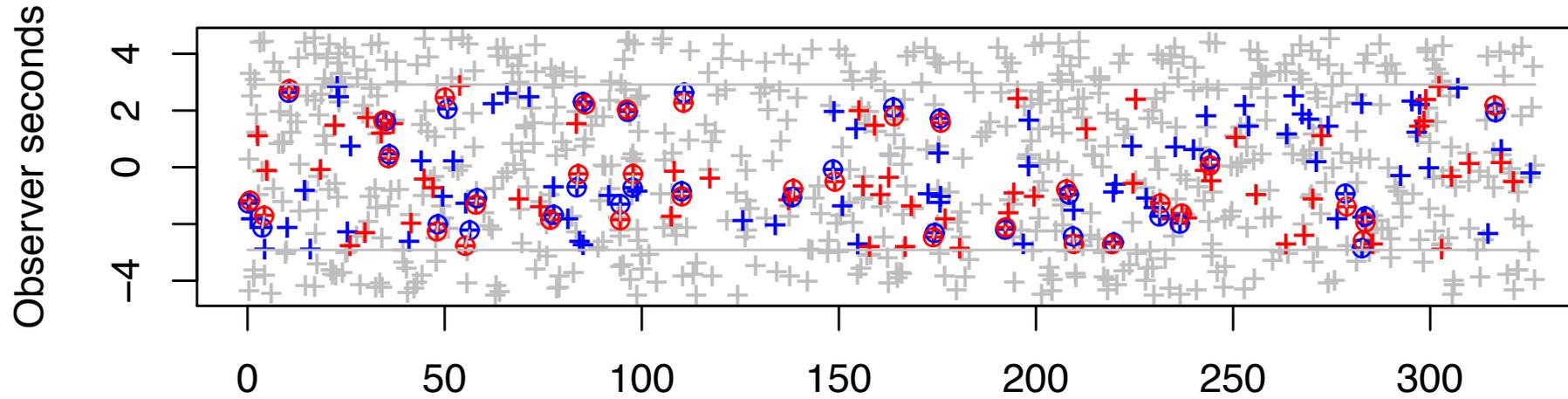
- Bracket "best" estimate by two extremes
- Rule-based duplicate identification after the survey. (e.g. Schweder et al., 1996)
- Probabilistic duplicate identification after the survey. (e.g. Hiby and Lovell, 1998, Stevenson *et al. submitted*)

Stevenson, B.C., Borchers, D.L. and Fewster, R.M. Cluster capture-recapture to account for identification uncertainty on aerial surveys of animal populations. (under revision for Biometrics).

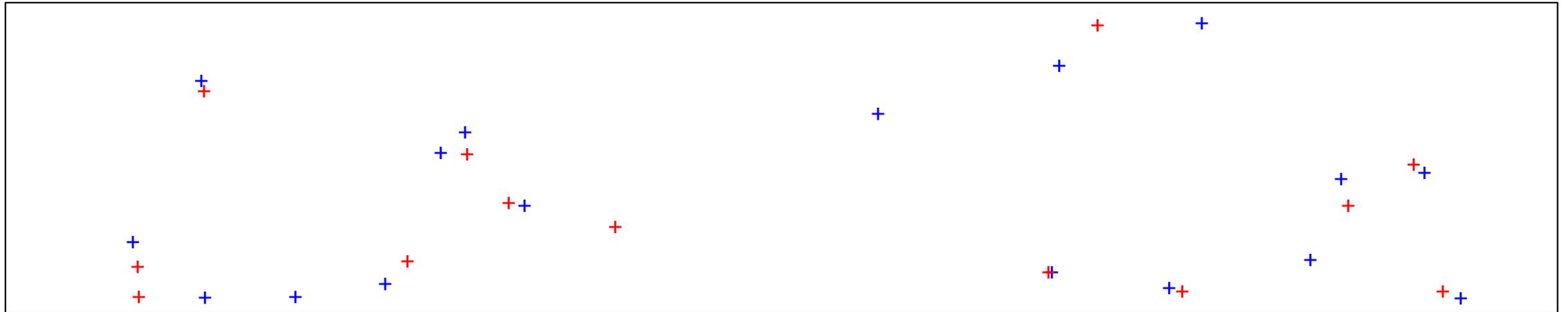
Schweder, T., Hagen, G., Helgeland, J. and Koppervik, I. 1996. Abundance estimation of northeastern Atlantic minke whales. *Rep. Int. Whal. Commn.* **46**: 391-405.

Hiby, A. and Lovell, P. 1998. Using aircraft in tandem formation to estimate abundance of harbour porpoise. *Biometrics* **54**: 1280-1289.

# Probabilistic Duplicate Identification



# Probabilistic Duplicate Identification



# Design to deal with availability bias

Use enough effort for certain detection at  $x=0$ : May not be possible

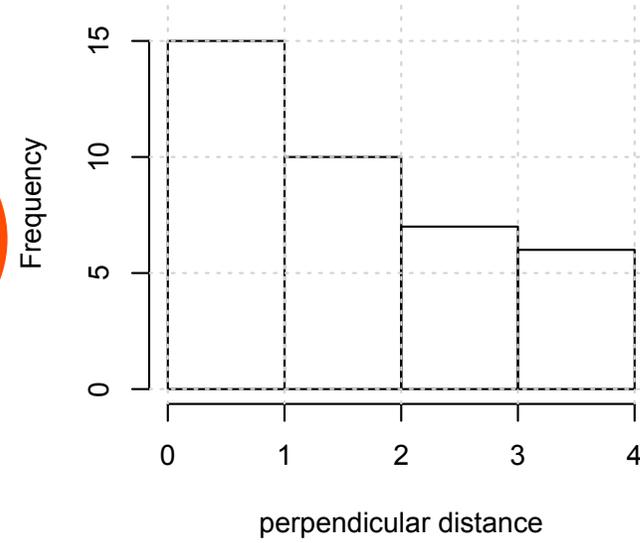
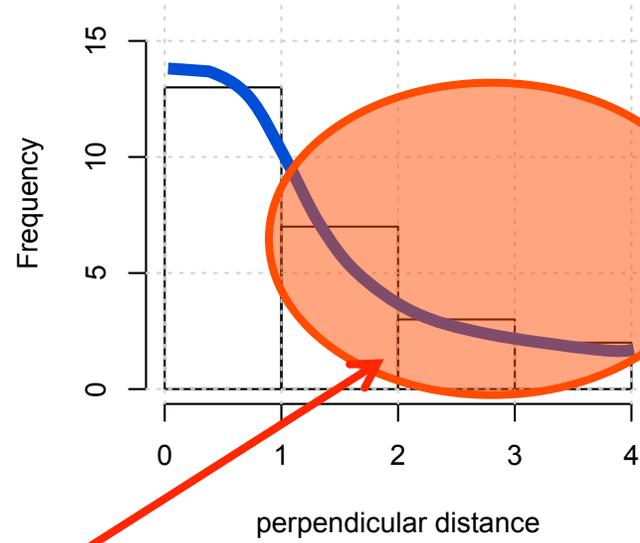
Use cue-based methods : Need to estimate availability process

Separate search areas of the observers (see pp 176-177 Adv. book)

Use different types of observers (e.g. visual and acoustic; visual and radio-tag)

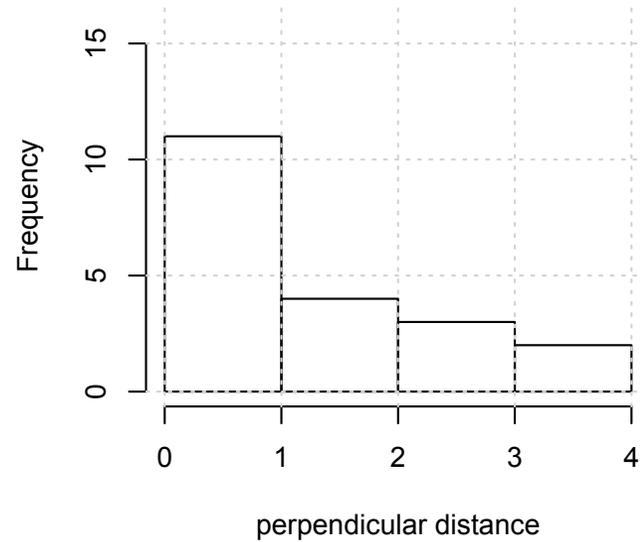
Availability bias correction factor: Need to be careful if animals in view for more than very small fraction of their availability cycle time.

Observer 1 (Ncnds=52) **Problem?** Observer 2

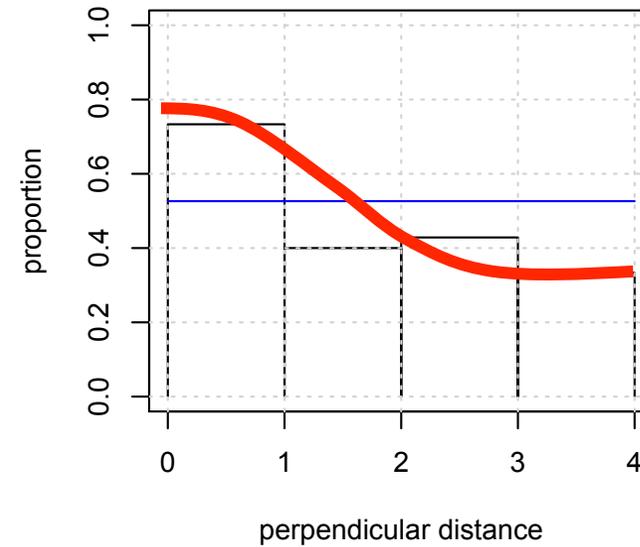


**Unmodelled Heterogeneity**  
here

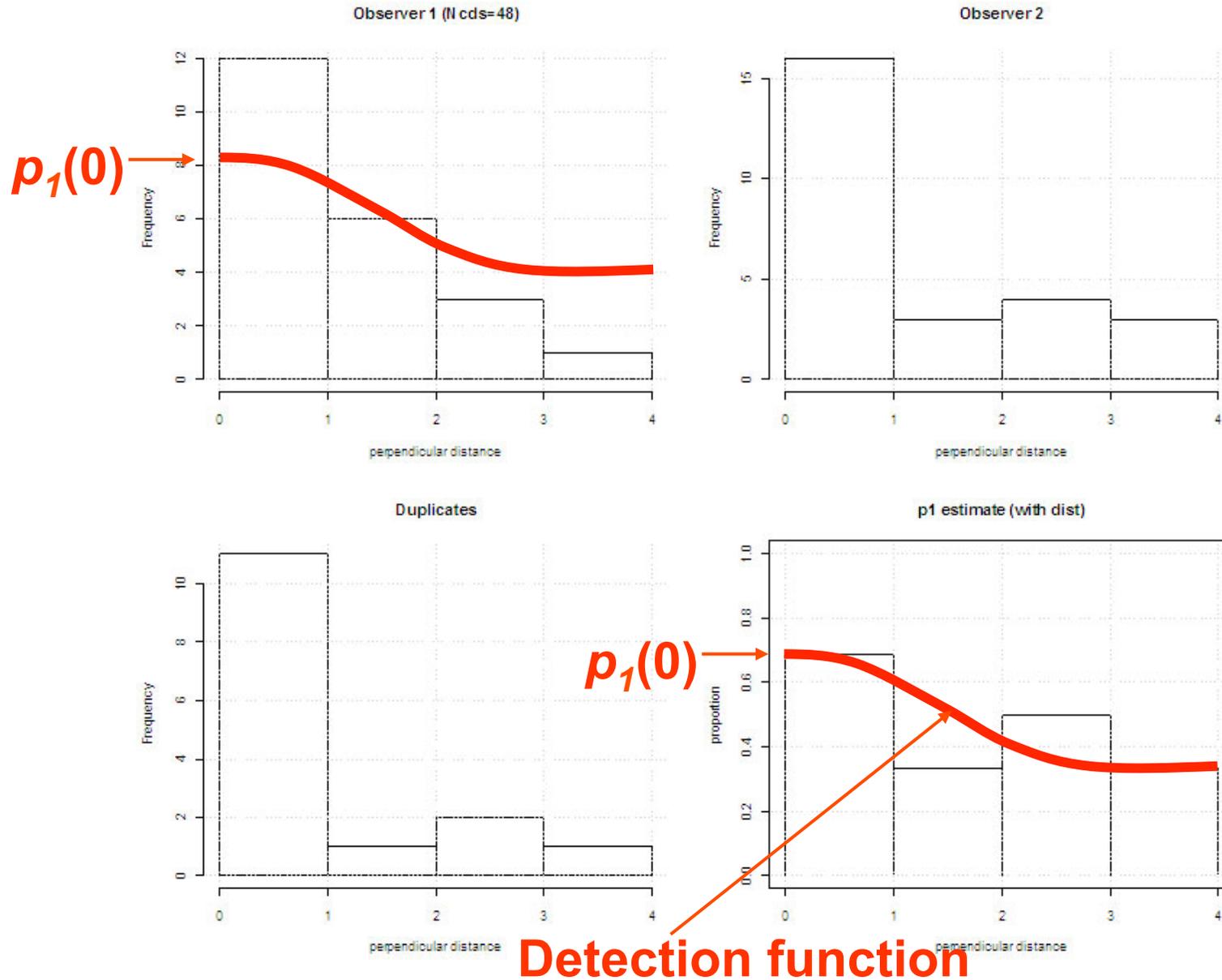
**Duplicates**



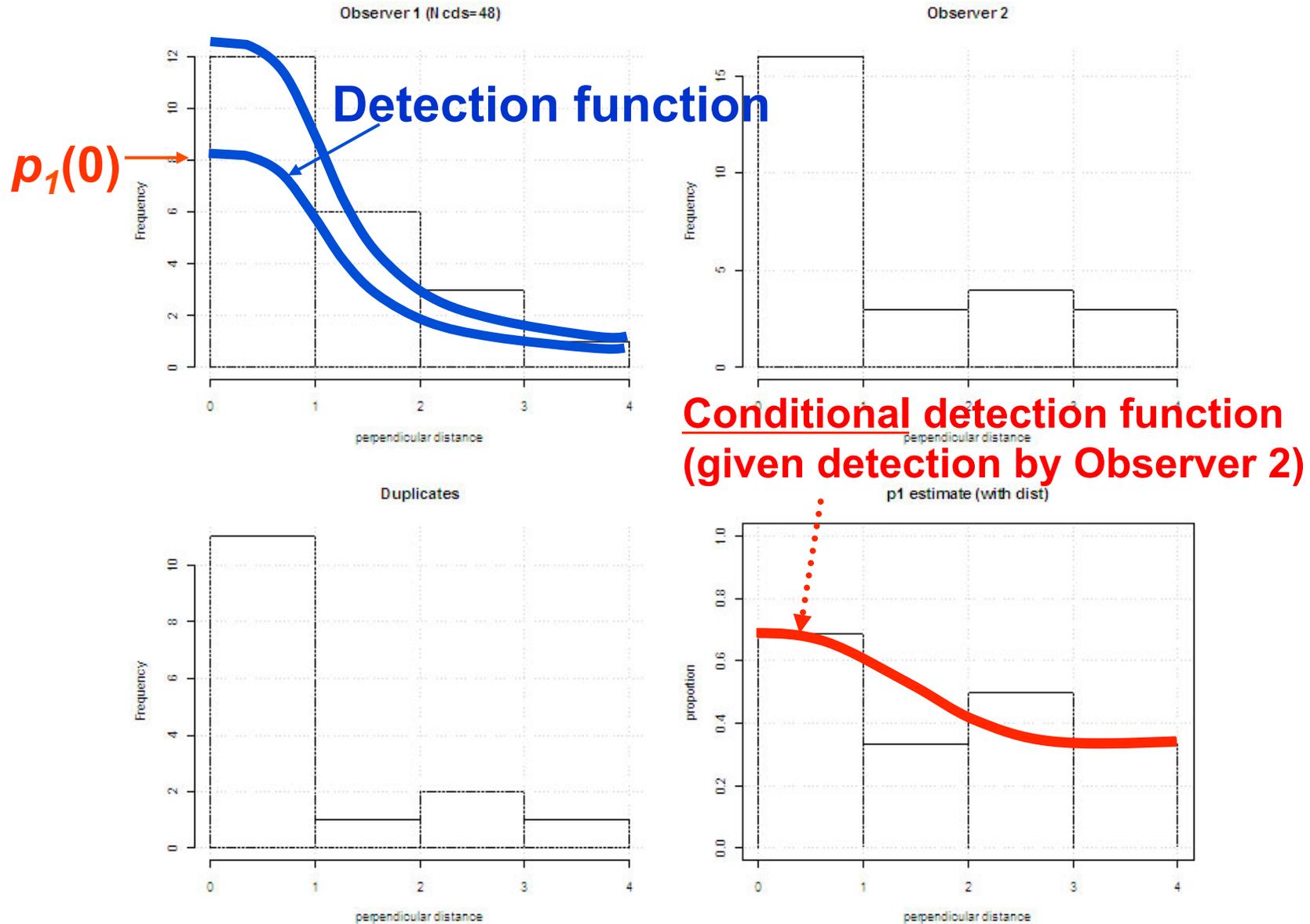
**p1 estimate (with dist)**



# Full Independence (FI) Model:



# Point Independence (PI) Model:



# Point vs Full Independence

## Full Independence

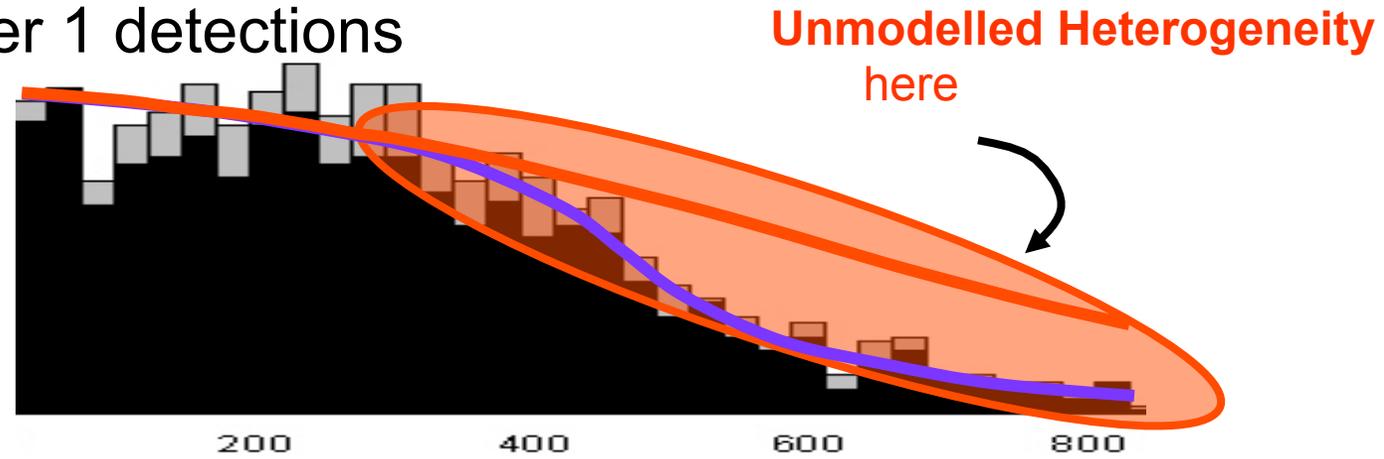
- Class e.g.  $N_{\text{hat}} = 48$ .
- Sensitive to unmodelled heterogeneity: negative bias.
- Assumption of uniform animal distribution not required - so useful if there is responsive movement.
- Don't use unless you have to.

## Point Independence

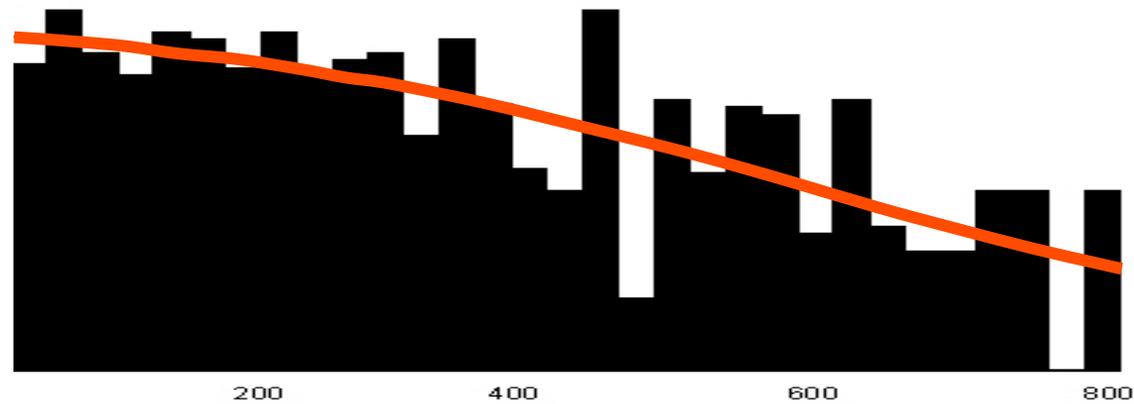
- Class e.g.  $N_{\text{hat}} = 70$ .
- Much less sensitive to unmodelled heterogeneity.
- Assumption of uniform animal distribution required – so no good if there is responsive movement.
- Use it unless there is responsive movement (or other non-uniform distribution).

# Example: Pack-Ice Seals

Observer 1 detections



**Proportion** of Observer 2 detections seen by Observer 1



# Sources of Heterogeneity

- The **animals** themselves (size, boldness)

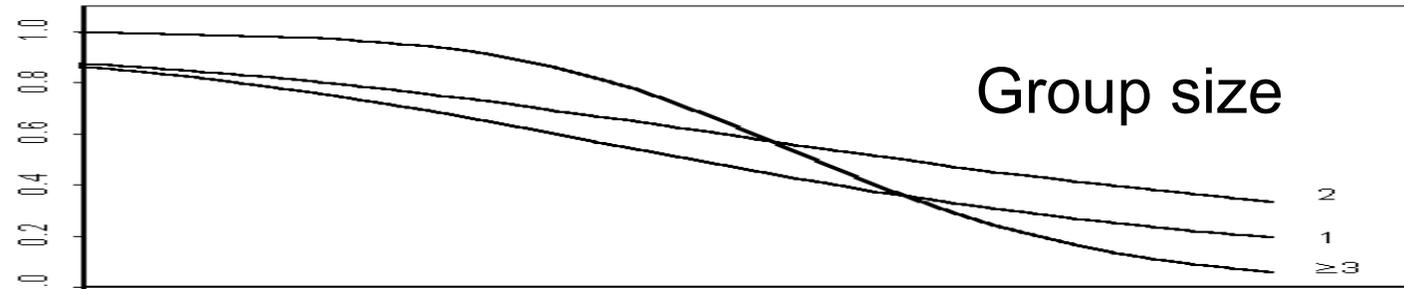
401	204	<b>404</b>
311		314
	<b>102</b>	
		212

- The **environment** (clear/"misty")

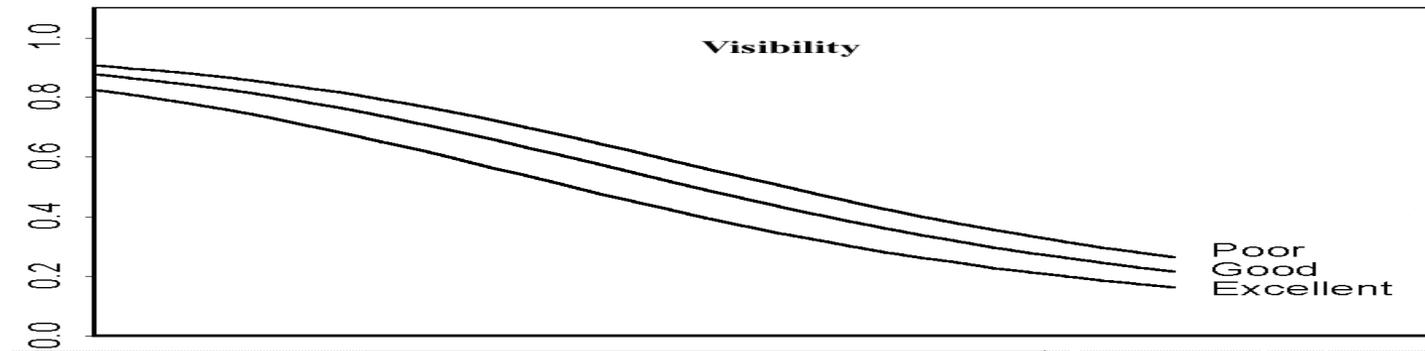
417	206		112
	118		113
		306	412
307	217		312
	218	416	104
			402

# Sources of Heterogeneity

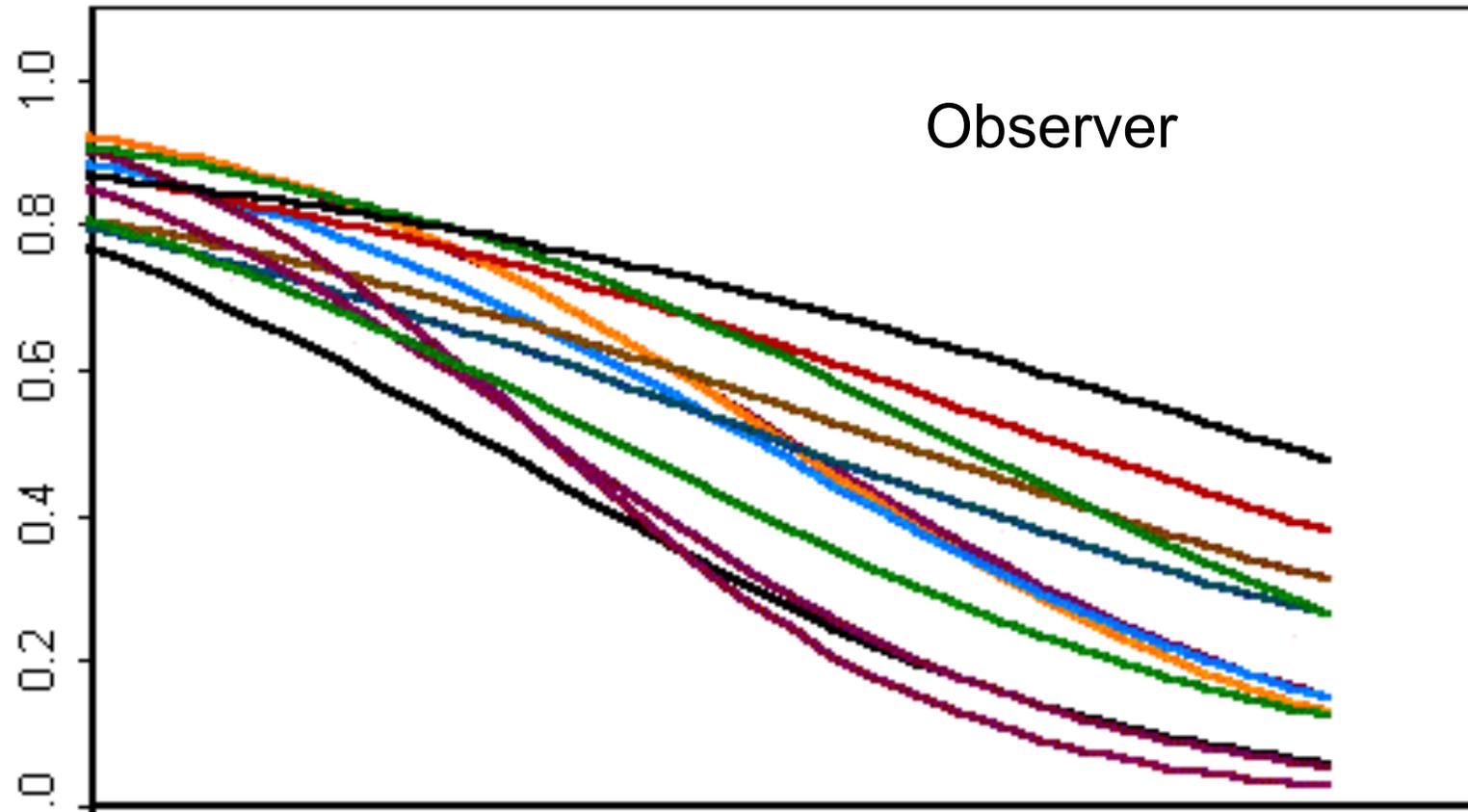
- The **animals** themselves (distance, size, availability, ...)



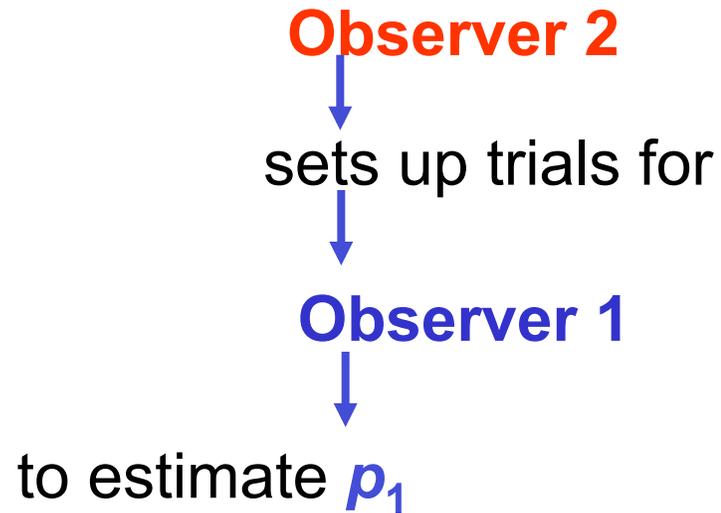
- The **environment** (sea state, ground cover, ...)



- The kind of **survey effort** (the observers, their platforms, ...)

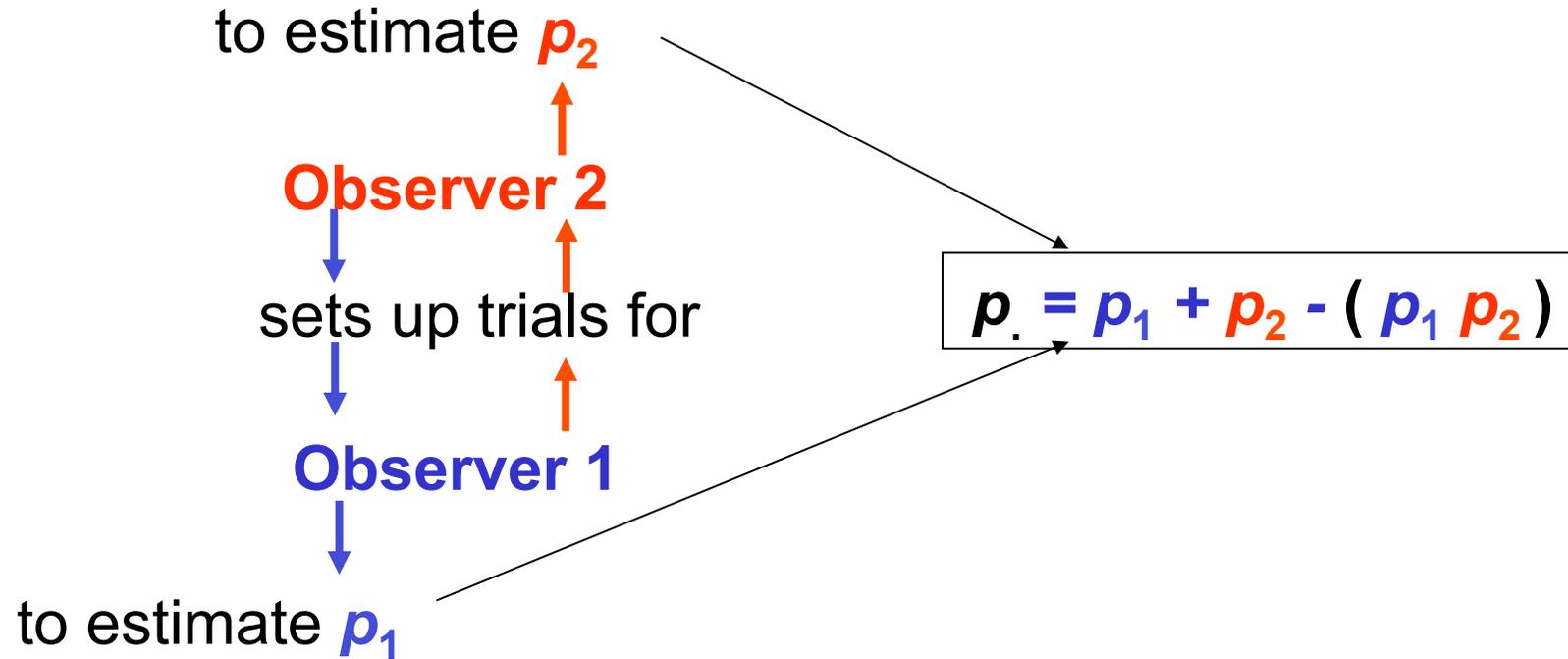


# Configuration: Trial-Observer



The Observer at the end of an arrow must be independent of the Observer at the start of the arrow

# Configuration: Independent Observer



The Observer at the end of an arrow must be independent of the Observer at the start of the arrow

# Abundance Estimation

- Trial-Observer  
...)

$$N = \sum_{i=1}^{\infty} \frac{1}{i^p} (x_i)$$

- Independent Observer  $N = \sum_{i=1}^{\infty} \frac{1}{i^p} (x_i, \dots)$

# Double-Platform Analysis Types

## Cue-based methods:

- Cues (not animals) are units; estimate  $p(\text{see cue})$
- Getting adequate estimates of cue generation process can be difficult.
- Able to incorporate heterogeneity due to availability (cue-ing) process.

- Animal-based methods:

We focus on these; in some applications cue-based methods perform better

- Animals are units; estimate  $p(\text{see animal})$
- Don't need to estimate availability/cue-ing process.
- More difficult to incorporate heterogeneity due to availability process.

# Related Models not covered:

## Limiting Independence

- Assume no unmodelled heterogeneity not at any point, but only as  $p$  approaches 1.
- See Buckland, S.T., Laake, J.L. and Borchers, D.L. 2009. Double-observer line transect methods: levels of independence. *Biometrics* **66**: 169-177

## Point Transects

- Can also do full, point and limiting independence with **Point Transects**.
- See Laake, J.L., Collier, B.A., Morrison, M.L. and Wilkins, R.N. 2011. Point-based mark-recapture distance sampling. *JABES* **16**: 389-408

# Critical Assumptions of Mark Recapture Line Transect

- Have the required independence between observers
- No unmodelled heterogeneity
- Duplicates (resightings) known (else need to include uncertainty in duplicate status in estimated variance)