Estimating precision of predictions from density surface models

Solution 7, Intermediate Distance Sampling workshop, CREEM, 2018

The analysis here is conditional on selecting a detection function and DSM in the previous exercises; I've shown a variety of models selected in the previous solutions to show the differences between models.

Much of the text below is as in the exercise itself, so it should be relatively easy to navigate.

Additional text and code is highlighted using boxes like this.

Now we've fitted some models and estimated abundance, we can estimate the variance associated with the abundance estimate (and plot it).

Load packages and data

```
library(dsm)
## Loading required package: mgcv
## Loading required package: nlme
## This is mgcv 1.8-24. For overview type 'help("mgcv-package")'.
## Loading required package: mrds
## This is mrds 2.2.0
## Built: R 3.5.1; ; 2018-08-03 20:22:18 UTC; windows
## Loading required package: numDeriv
## This is dsm 2.2.16
## Built: R 3.4.2; ; 2017-11-02 15:05:30 UTC; windows
library(raster)
## Loading required package: sp
##
## Attaching package: 'raster'
## The following object is masked from 'package:nlme':
##
##
       getData
library(ggplot2)
library(viridis)
## Loading required package: viridisLite
library(plyr)
library(knitr)
library(rgdal)
## rgdal: version: 1.3-4, (SVN revision 766)
## Geospatial Data Abstraction Library extensions to R successfully loaded
## Loaded GDAL runtime: GDAL 2.2.3, released 2017/11/20
## Path to GDAL shared files: C:/Users/louise/Documents/R/win-library/3.5/rgdal/gdal
## GDAL binary built with GEOS: TRUE
```

```
## Loaded PROJ.4 runtime: Rel. 4.9.3, 15 August 2016, [PJ_VERSION: 493]
## Path to PROJ.4 shared files: C:/Users/louise/Documents/R/win-library/3.5/rgdal/proj
## Linking to sp version: 1.3-1

Load the models and prediction grid:
load("dsms.RData")
load("dsms-xy.RData")
load("predgrid.RData")
```

Estimation of variance

Depending on the model response (count or Horvitz-Thompson) we can use either dsm.var.prop or dsm.var.gam, respectively. dsm_nb_xy_ms doesn't include any covariates at the observer level in the detection function, so we can use the variance propagation method and estimate the uncertainty in detection function parameters in one step.

```
# need to remove the NAs as we did when plotting
predgrid_var <- predgrid[!is.na(predgrid$Depth),]</pre>
# now estimate variance
var_nb_xy_ms <- dsm.var.prop(dsm_nb_xy_ms, predgrid_var, off.set=predgrid_var$off.set)</pre>
## Warning in dsm_varprop(dsm.obj, pred.data[[1]]): Model was fitted using
## nb() family, refitting with negbin(). See ?dsm_varprop
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To summarise the results of this variance estimate:
summary(var_nb_xy_ms)
## Summary of uncertainty in a density surface model calculated
## by variance propagation.
## Probability of detection in fitted model and variance model
## [1] Fitted.model
                      Fitted.model.se Refitted.model
## <0 rows> (or 0-length row.names)
## Approximate asymptotic confidence interval:
##
       2.5%
                Mean
                        97.5%
## 1139.292 1588.874 2215.867
## (Using log-Normal approximation)
                                  : 1588.874
## Point estimate
## Standard error
                                  : 271.5953
## Coefficient of variation
                                  : 0.1709
```

Try this out for some of the other models you've saved. Remember to use dsm.var.gam when there are covariates in the detection function and dsm.var.prop when there aren't.

We'll skip this and go straight to summarising all our models so far in the next section...

Summarise multiple models

We can again summarise all the models, as we did with the DSMs and detection functions, now including the variance:

```
summarize_dsm_var <- function(model, predgrid){</pre>
  summ <- summary(model)</pre>
  vp <- summary(dsm.var.prop(model, predgrid, off.set=predgrid$off.set))</pre>
  unconditional.cv.square <- vp$cv^2
  asymp.ci.c.term <- exp(1.96*sqrt(log(1+unconditional.cv.square)))
  asymp.tot <- c(vp$pred.est / asymp.ci.c.term,</pre>
                 vp$pred.est,
                 vp$pred.est * asymp.ci.c.term)
  data.frame(response = model$family$family,
             terms = paste(rownames(summ$s.table), collapse=", "),
             AIC
                      = AIC(model),
                      = model$gcv.ubre,
             "Dev_exp" = paste0(round(summ$dev.expl*100,1),"%"),
             "low_CI" = round(asymp.tot[1],2),
             "Nhat" = round(asymp.tot[2],2),
             "up_CI" = round(asymp.tot[3],2)
             )
```

This takes a long time!

```
# make a list of models
model_list <- list(dsm_nb_xy, dsm_nb_x_y, dsm_nb_xy_ms, dsm_nb_x_y_ms,</pre>
                           dsm_tw_xy, dsm_tw_xy, dsm_tw_xy_ms, dsm_tw_x_y_ms)
# give the list names for the models, so we can identify them later
names(model_list) <- c("dsm_nb_xy", "dsm_nb_xy", "dsm_nb_xy_ms", "dsm_nb_xy_ms",</pre>
                           "dsm_tw_xy", "dsm_tw_x_y", "dsm_tw_xy_ms", "dsm_tw_xy_ms")
per_model_var <- ldply(model_list, summarize_dsm_var, predgrid=predgrid_var)</pre>
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## nb() family, refitting with negbin(). See ?dsm_varprop
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kable(per_model_var, digits=1, booktabs=TRUE)
```

.id	response	terms	AIC	REML	Dev_exp	low_CI	Nhat	up_
dsm_nb_xy	Negative Binomial(0.089)	s(x,y)	787.9	285.5	34.7%	1084.8	1611.5	239
$dsm_nb_x_y$	Negative Binomial(0.08)	s(x), s(y)	792.5	286.1	29.6%	1089.0	1581.2	229
$dsm_nb_xy_ms$	Negative $Binomial(0.105)$	s(x,y), s(Depth)	758.4	278.2	37.4%	1139.3	1588.9	221
$dsm_nb_x_y_ms$	Negative Binomial(0.096)	s(y), s(Depth)	762.9	278.7	35.6%	1148.4	1615.5	227
dsm_tw_xy	Tweedie($p=1.295$)	s(x,y)	1250.3	287.0	32%	1274.5	1743.0	238
dsm_tw_x_y	Tweedie($p=1.309$)	s(x), s(y)	1252.1	289.1	25.7%	1225.0	1670.8	227
dsm_tw_xy_ms	Tweedie($p=1.283$)	s(x,y), $s(Depth)$	1225.9	279.8	33.4%	1212.6	1623.1	217
dsm_tw_x_y_ms	Tweedie $(p=1.285)$	s(Depth), s(NPP)	1227.9	281.3	34.3%	738.7	1201.8	195

Plotting

We can plot a map of the coefficient of variation, but we first need to estimate the variance per prediction cell, rather than over the whole area. This calculation takes a while!

```
# use the split function to make each row of the predictiond data.frame into
# an element of a list
predgrid_var_split <- split(predgrid_var, 1:nrow(predgrid_var))
var_split_nb_xy_ms <- dsm.var.prop(dsm_nb_xy_ms, predgrid_var_split, off.set=predgrid_var_soff.set)

## Warning in dsm_varprop(dsm.obj, pred.data[[1]]): Model was fitted using
## nb() family, refitting with negbin(). See ?dsm_varprop

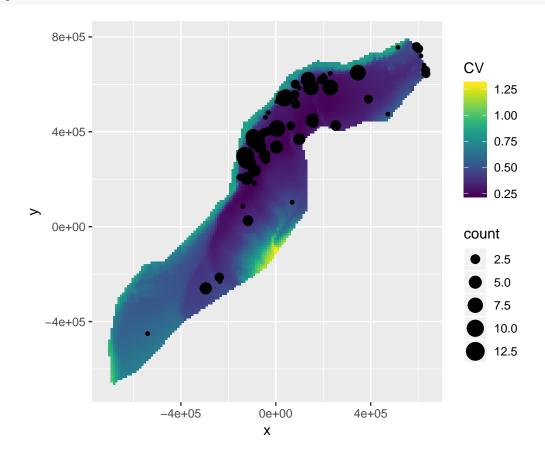
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```

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```

Now we have the per-cell coefficients of variation, we assign that to a column of the prediction grid data and plot it as usual:



Note that here we overplot the segments where sperm whales were observed (and scale the size of the point according to the number observed), using <code>geom_point()</code>.

Try this with the other models you fitted and see what the differences are between the maps of coefficient of variation.

We can use a similar technique as we did in the prediction exercises to get coefficient of variation maps for all of the models...

Note this can take a long time!

```
# make a function that calculates the CV, adds them to a column named CV
# and adds a column called "model" that stores the model name, then returns the
# data.frame.
make_cv_dat <- function(model_name, predgrid_split, predgrid){
    # we use get() here to grab the object with the name of its argument</pre>
```

```
var_obj <- dsm.var.prop(get(model_name), predgrid_split, off.set=predgrid$off.set)</pre>
  predgrid[["CV"]] <- sqrt(var_obj$pred.var)/unlist(var_obj$pred)</pre>
  predgrid[["model"]] <- model_name</pre>
 return(predgrid)
}
# load plyr and apply to a list of the names of the models, make_cv_dat returns
# a data.frame (hence this is an "ld" function: list->data.frame) that it then binds
# together
library(plyr)
big_cv <- ldply(list("dsm_nb_xy", "dsm_nb_xy", "dsm_nb_xy_ms", "dsm_nb_xy_ms",
                     "dsm_tw_xy", "dsm_tw_x_y", "dsm_tw_xy_ms", "dsm_tw_x_y_ms"),
                make_cv_dat, predgrid_split=predgrid_var_split, predgrid=predgrid_var_map)
## Warning in dsm_varprop(dsm.obj, pred.data[[1]]): Model was fitted using
## nb() family, refitting with negbin(). See ?dsm_varprop
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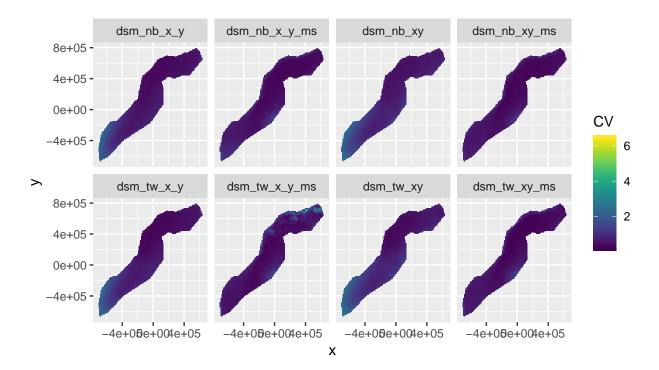
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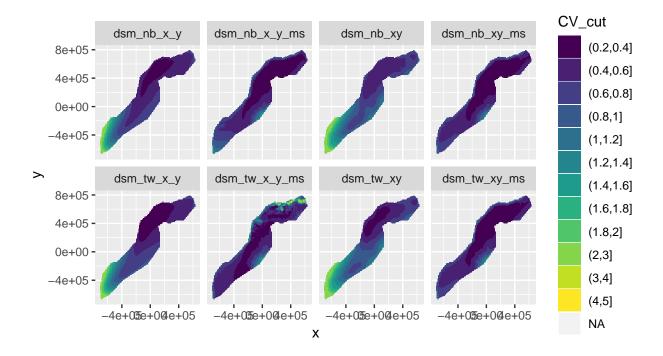
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p <- ggplot(big_cv) +</pre>
       geom_tile(aes(x=x, y=y, fill=CV, width=10*1000, height=10*1000)) +
       scale_fill_viridis() +
       coord_equal() +
```

```
facet_wrap(~model, nrow=2)
print(p)
```



One issue with producing this kind of plot is that ggplot2 will use a common legend, meaning if there are some cells with high values, this can throw out the rest of the scale.

As suggested in the lectures, we'll now use cut() to create a categorised version of the CV and plot that instead:



This is a bit easier to read.

Save the uncertainty maps to raster files

As with the predictions, we'd like to save our uncertainty estimates to a raster layer so we can plot them in GIS. Again, this involves a bit of messing about with the data format before we can save.

```
# setup the storage for the cvs
cv_raster <- raster(predictorStack)
# we removed the NA values to make the predictions and the raster needs them
# so make a vector of NAs, and insert the CV values...
cv_na <- rep(NA, nrow(predgrid))
cv_na[!is.na(predgrid$Depth)] <- cv
# put the values in, making sure they are numeric first
cv_raster <- setValues(cv_raster, cv_na)
# name the new, last, layer in the stack
names(cv_raster) <- "CV_nb_xy"</pre>
```

We can then save that object to disk as a raster file:

```
writeRaster(cv_raster, "cv_raster.img", datatype="FLT4S")
```